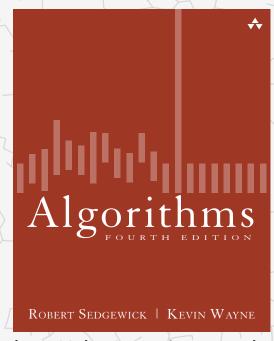
Algorithms



http://algs4.cs.princeton.edu

6.6 INTRACTABILITY

- introduction
- search problems
- Pvs. NP
- classifying problems
- NP-completeness
- coping with intractability



introduction

search problems

Pvs. NP

classifying problems

NP-completeness

coping with intractability

Algorithms

ROBERT SEDGEWICK | KEVIN WAYNE

http://algs4.cs.princeton.edu

Questions about computation

- Q. What is a general-purpose computer?
- Q. Are there limits on the power of digital computers?
- Q. Are there limits on the power of machines we can build?



David Hilbert



Kurt Gödel



Alan Turing



Alonzo Church



John von Neumann

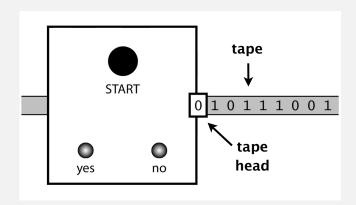
A simple model of computation: DFAs

Tape.

- Stores input.
- One arbitrarily long strip, divided into cells.
- Finite alphabet of symbols.

Tape head.

- Points to one cell of tape.
- · Reads a symbol from active cell.
- Moves one cell at a time.





- Q. Is there a more powerful model of computation?
- A. Yes.

A universal model of computation: Turing machines

Tape.

- Stores input, output, and intermediate results.
- One arbitrarily long strip, divided into cells.
- Finite alphabet of symbols.

Tape head.

- Points to one cell of tape.
- Reads a symbol from active cell.
- Writes a symbol to active cell.
- Moves one cell at a time.



Q. Is there a more powerful model of computation?

A. No! ← most important scientific result of 20th century?

tape head

START

RESET

tape

Church-Turing thesis (1936)

Turing machines can compute any function that can be computed by a physically harnessable process of the natural world.

Remark. "Thesis" and not a mathematical theorem because it's a statement about the physical world and not subject to proof.

but can be falsified

Use simulation to prove models equivalent.

- Android simulator on iPhone.
- iPhone simulator on Android.

Implications.

- No need to seek more powerful machines or languages.
- Enables rigorous study of computation (in this universe).

Bottom line. Turing machine is a simple and universal model of computation.

Church-Turing thesis: evidence

• 8 decades without a counterexample.



• Many, many models of computation that turned out to be equivalent.

model of computation	description		
enhanced Turing machines	multiple heads, multiple tapes, 2D tape, nondeterminism		
untyped lambda calculus	method to define and manipulate functions		
recursive functions	functions dealing with computation on integers		
unrestricted grammars	iterative string replacement rules used by linguists		
extended L-systems	parallel string replacement rules that model plant growth		
programming languages	Java, C, C++, Perl, Python, PHP, Lisp, PostScript, Excel		
random access machines	registers plus main memory, e.g., TOY, Pentium		
cellular automata	cells which change state based on local interactions		
quantum computer	compute using superposition of quantum states		
DNA computer	compute using biological operations on DNA		

A question about algorithms

- Q. Which algorithms are useful in practice?
 - Measure running time as a function of input size N.
 - Useful in practice ("efficient") = polynomial time for all inputs.





von Neumann (1953)



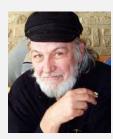
Nash (1955)



Gödel (1956)



Cobham (1964)



Edmonds (1965)



Rabin (1966)

- Ex 1. Sorting N items takes $N \log N$ compares using mergesort.
- Ex 2. Finding best TSP tour on N points takes N! steps using brute search.

Theory. Definition is broad and robust.

constants a and b tend to be small, e.g., $3N^2$

Practice. Poly-time algorithms scale to huge problems.

Exponential growth

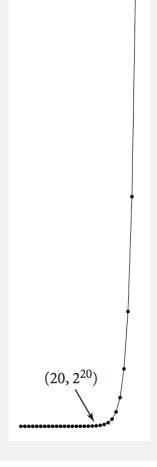
Exponential growth dwarfs technological change.

- Suppose you have a giant parallel computing device...
- With as many processors as electrons in the universe...
- And each processor has power of today's supercomputers...
- And each processor works for the life of the universe...

quantity	value
electrons in universe †	1079
supercomputer instructions per second †	1013
age of universe in seconds †	1017
+	ostimatod

• Will not help solve 1,000 city TSP problem via brute force.





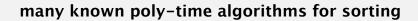
 $(30, 2^{30})$

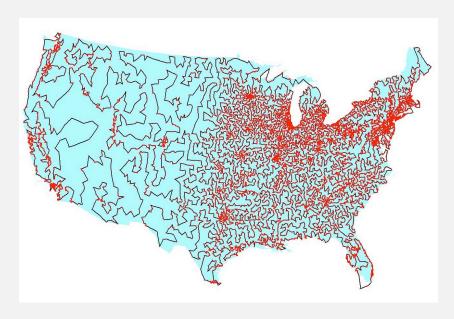
Questions about problems

- Q. Which problems can we solve in practice?
- A. Those with poly-time algorithms.
- Q. Which problems have poly-time algorithms?
- A. Not so easy to know. Focus of today's lecture.









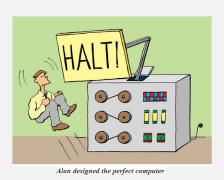
no known poly-time algorithm for TSP

Bird's-eye view

Def. A problem is intractable if it can't be solved in polynomial time. Desiderata. Prove that a problem is intractable.

Two problems that provably require exponential time.

- Given a constant-size program, does it halt in at most *K* steps?
- Given N-by-N checkers board position, can the first player force a win?





using forced capture rule

input size = $c + \lg K$

Frustrating news. Very few successes.



introduction

search problems

Pvs. NP

classifying problems

NP-completeness

coping with intractability

Algorithms

Robert Sedgewick | Kevin Wayne

http://algs4.cs.princeton.edu



- introduction
- search problems
 - P vs. NP
- classifying problems
 - NP-completeness
- coping with intractability

Algorithms

ROBERT SEDGEWICK | KEVIN WAYNE

http://algs4.cs.princeton.edu

Four fundamental problems

LSOLVE. Given a system of linear equations, find a solution.

$$x_0 = -1$$

 $x_1 = 2$
 $x_2 = 2$ variables are real numbers

Given a system of linear inequalities, find a solution.

$$48x_0 + 16x_1 + 119x_2 \le 88$$

$$5x_0 + 4x_1 + 35x_2 \ge 13$$

$$15x_0 + 4x_1 + 20x_2 \ge 23$$

$$x_0 , x_1 , x_2 \ge 0$$

$$x_0 = 1$$
 $x_1 = 1$
 $x_2 = \frac{1}{5}$

variables are real numbers

ILP. Given a system of linear inequalities, find a 0-1 solution.

$$x_1 + x_2 \ge 1$$
 $x_0 + x_1 + x_2 \ge 1$
 $x_0 + x_1 + x_2 \le 2$

$$x_0 = 0$$
 $x_1 = 1$
 $x_2 = 1$

variables are 0 or 1

SAT. Given a system of boolean equations, find a binary solution.

$$(x'_1 or x'_2)$$
 and $(x_0 or x_2) = true$
 $(x_0 or x_1)$ and $(x_1 or x'_2) = false$
 $(x_0 or x_2)$ and $(x'_0) = true$

$$x_0 = false$$
 variables are true or false $x_1 = false$ $x_2 = true$

Four fundamental problems

- LSOLVE. Given a system of linear equations, find a solution.
- LP. Given a system of linear inequalities, find a solution.
- ILP. Given a system of linear inequalities, find a 0-1 solution.
- SAT. Given a system of boolean equations, find a binary solution.

- Q. Which of these problems have poly-time algorithms?
 - LSOLVE. Yes. Gaussian elimination solves N-by-N system in N^3 time.
 - LP. Yes. Ellipsoid algorithm is poly-time. but was open problem for decades
 - ILP, SAT. No poly-time algorithm known or believed to exist!



Search problem. Given an instance I of a problem, find a solution S. Requirement. Must be able to efficiently check that S is a solution.

or report

poly-time in size of instance I



Search problem. Given an instance *I* of a problem, find a solution *S*. Requirement. Must be able to efficiently check that *S* is a solution.

LSOLVE. Given a system of linear equations, find a solution.

$$0x_0 + 1x_1 + 1x_2 = 4$$
 $x_0 = -1$
 $2x_0 + 4x_1 - 2x_2 = 2$ $x_1 = 2$
 $0x_0 + 3x_1 + 15x_2 = 36$ $x_2 = 2$

$$x_0 = -1$$

$$x_1 = 2$$

instance I

solution S

To check solution S, plug in values and verify each equation.

Search problem. Given an instance I of a problem, find a solution S. Requirement. Must be able to efficiently check that S is a solution.

LP. Given a system of linear inequalities, find a solution.

$$48x_{0} + 16x_{1} + 119x_{2} \le 88$$

$$5x_{0} + 4x_{1} + 35x_{2} \ge 13$$

$$15x_{0} + 4x_{1} + 20x_{2} \ge 23$$

$$x_{0} , x_{1} , x_{2} \ge 0$$

$$x_{0} = 1$$

$$x_{1} = 1$$

$$x_{2} = \frac{1}{5}$$

instance I

solution S

To check solution S, plug in values and verify each inequality.

Search problem. Given an instance *I* of a problem, find a solution *S*. Requirement. Must be able to efficiently check that *S* is a solution.

ILP. Given a system of linear inequalities, find a binary solution.

$$x_1 + x_2 \ge 1$$
 $x_0 = 0$
 $x_0 + x_2 \ge 1$ $x_1 = 1$
 $x_0 + x_1 + x_2 \le 2$ $x_2 = 1$

$$x_0 = 0$$

$$x_1 = 1$$

$$x_2 = 1$$

instance I

solution S

To check solution S, plug in values and verify each inequality.

Search problem. Given an instance I of a problem, find a solution S. Requirement. Must be able to efficiently check that S is a solution.

SAT. Given a system of boolean equations, find a boolean solution.

solution S

$$(x'_1 \text{ or } x'_2)$$
 and $(x_0 \text{ or } x_2) = true$ $x_0 = false$ $(x_0 \text{ or } x_1)$ and $(x_1 \text{ or } x'_2) = false$ $x_1 = false$ $x_2 = true$

instance I

To check solution S, plug in values and verify each equation.

Search problem. Given an instance I of a problem, find a solution S. Requirement. Must be able to efficiently check that S is a solution.

FACTOR. Given an *n*-bit integer *x*, find a nontrivial factor.

input size = number of bits

147573952589676412927

193707721

instance I

solution S

To check solution *S*, long divide 193707721 into 147573952589676412927.



- introduction
- search problems
 - P vs. NP
- classifying problems
 - NP-completeness
- coping with intractability

Algorithms

ROBERT SEDGEWICK | KEVIN WAYNE

http://algs4.cs.princeton.edu



introduction

search problems

P vs. NP

classifying problems

NP-completeness

coping with intractability

Algorithms

ROBERT SEDGEWICK | KEVIN WAYNE

http://algs4.cs.princeton.edu

Def. NP is the class of all search problems. ←

Note: classic definition limits

NP to yes-no problems

problem	description	poly-time algorithm	instance I	solution S
LSOLVE (A, b)	Find a vector x that satisfies $Ax = b$	Gaussian elimination	$0x_0 + 1x_1 + 1x_2 = 4$ $2x_0 + 4x_1 - 2x_2 = 2$ $0x_0 + 3x_1 + 15x_2 = 36$	$x_0 = -1$ $x_1 = 2$ $x_2 = 2$
LP (A, b)	Find a vector x that satisfies $Ax \le b$	ellipsoid	$48x_0 + 16x_1 + 119x_2 \le 88$ $5x_0 + 4x_1 + 35x_2 \ge 13$ $15x_0 + 4x_1 + 20x_2 \ge 23$ $x_0 , x_1 , x_2 \ge 0$	$x_0 = 1$ $x_1 = 1$ $x_2 = \frac{1}{5}$
ILP (A, b)	Find a binary vector x that satisfies $Ax \le b$???	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$x_0 = 0$ $x_1 = 1$ $x_2 = 1$
SAT (Φ, <i>b</i>)	Find a boolean vector x that satisfies $\Phi(x) = b$???	$(x'_1 or x'_2) and (x_0 or x_2) = true$ $(x_0 or x_1) and (x_1 or x'_2) = false$ $(x_0 or x_2) and (x'_0) = true$	$x_0 = false$ $x_1 = false$ $x_2 = true$
FACTOR (x)	Find a nontrivial factor of the integer <i>x</i>	???	147573952589676412927	193707721

Significance. What scientists and engineers aspire to compute feasibly.

Def. P is the class of search problems solvable in poly-time.

Note: classic definition limits
P to yes-no problems

problem	description	poly-time algorithm	instance I	solution S
LSOLVE (A, b)	Find a vector x that satisfies $Ax = b$	Gaussian elimination (Edmonds 1967)	$0x_0 + 1x_1 + 1x_2 = 4$ $2x_0 + 4x_1 - 2x_2 = 2$ $0x_0 + 3x_1 + 15x_2 = 36$	$x_0 = -1$ $x_1 = 2$ $x_2 = 2$
LP (A, b)	Find a vector x that satisfies $Ax \le b$	ellipsoid (Khachiyan 1979)	$48x_0 + 16x_1 + 119x_2 \le 88$ $5x_0 + 4x_1 + 35x_2 \ge 13$ $15x_0 + 4x_1 + 20x_2 \ge 23$ $x_0 , x_1 , x_2 \ge 0$	$x_0 = 1$ $x_1 = 1$ $x_2 = \frac{1}{5}$
SORT (a)	Find a permutation that puts array a in order	mergesort (von Neumann 1945)	2.3 8.5 1.2 9.1 2.2 0.3	5 2 4 0 1 3
STCONN (<i>G, s, t</i>)	Find a path in a graph G from s to t	depth-first search (Theseus)		

Significance. What scientists and engineers do compute feasibly.

Nondeterminism

Nondeterministic machine can guess the desired solution.

recall NFA implementation

- Java: initializes entries to 0.
- Nondeterministic machine: initializes entries to the solution!
- ILP. Given a system of linear inequalities, guess a 0-1 solution.

$$x_1 + x_2 \ge 1$$
 $x_0 + x_1 + x_2 \ge 1$
 $x_0 + x_1 + x_2 \le 2$

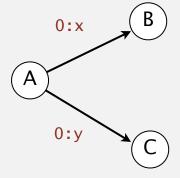
$$x_0 = 0$$

$$x_1 = 1$$

$$x_2 = 1$$

Ex. Turing machine.

- Deterministic: state, input determines next state.
- Nondeterministic: more than one possible next state.



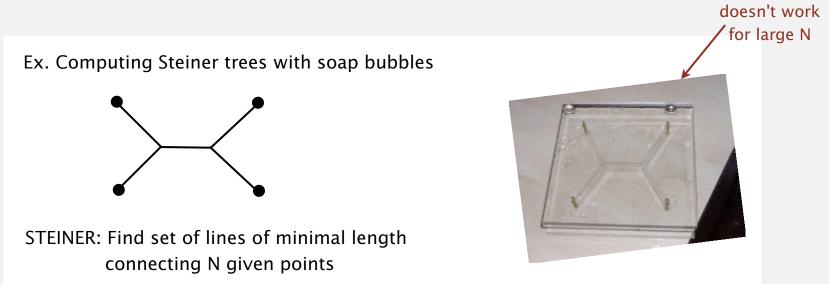
NP. Search problems solvable in poly time on a nondeterministic TM.

Extended Church-Turing thesis

P = search problems solvable in poly-time in the natural world.

Evidence supporting thesis. True for all physical computers.

Natural computers? No successful attempts (yet).



Implication. To make future computers more efficient, suffices to focus on improving implementation of existing designs.

P vs. NP

Does P = NP?



Copyright © 1990, Matt Groening

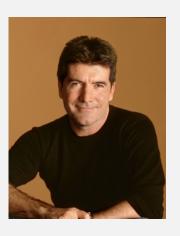


Copyright © 2000, Twentieth Century Fox

Automating creativity

- Q. Being creative vs. appreciating creativity?
- Ex. Mozart composes a piece of music; our neurons appreciate it.
- Ex. Wiles proves a deep theorem; a colleague referees it.
- Ex. Boeing designs an efficient airfoil; a simulator verifies it.
- Ex. Einstein proposes a theory; an experimentalist validates it.





ordinary

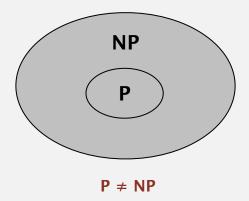
Computational analog. Does P = NP?

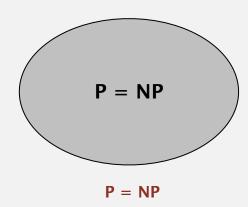
The central question

- P. Class of search problems solvable in poly-time.
- NP. Class of all search problems.

Does P = NP? [Can you always avoid brute-force searching and do better]

Two worlds.





If P = NP... Poly-time algorithms for SAT, ILP, TSP, FACTOR, ...

If $P \neq NP...$ Would learn something fundamental about our universe.

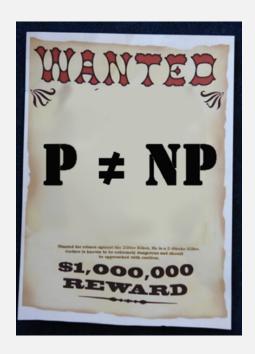
Overwhelming consensus. $P \neq NP$.

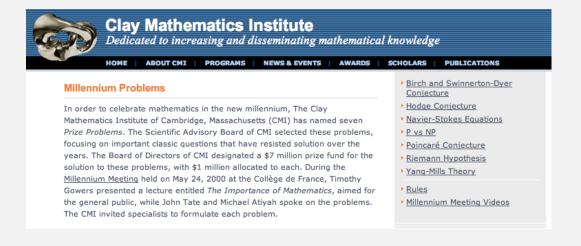
The central question

- P. Class of search problems solvable in poly-time.
- NP. Class of all search problems.

Does P = NP? [Can you always avoid brute-force searching and do better]

Millennium prize. 1 million for resolution of P = NP problem.







introduction

search problems

P vs. NP

classifying problems

NP-completeness

coping with intractability

Algorithms

ROBERT SEDGEWICK | KEVIN WAYNE

http://algs4.cs.princeton.edu



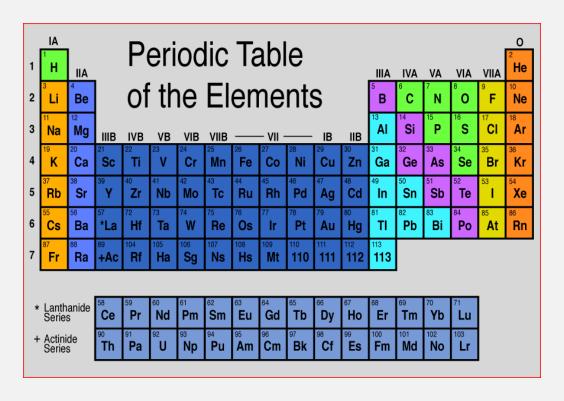
- introduction
- search problems
- Pvs. NP
- classifying problems
- NP-completeness
- coping with intractability

Algorithms

ROBERT SEDGEWICK | KEVIN WAYNE

http://algs4.cs.princeton.edu

Periodic table of the elements



A key problem: satisfiability

SAT. Given a system of boolean equations, find a solution.

$$x'_1 ext{ or } x_2 ext{ or } x_3 = true$$

 $x_1 ext{ or } x'_2 ext{ or } x_3 = true$
 $x'_1 ext{ or } x'_2 ext{ or } x'_3 = true$
 $x'_1 ext{ or } x'_2 ext{ or } x_4 = true$

Key applications.

- Automatic verification systems for software.
- Electronic design automation (EDA) for hardware.
- Mean field diluted spin glass model in physics.

• ...

Exhaustive search

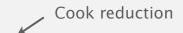
- Q. How to solve an instance of SAT with *n* variables?
- A. Exhaustive search: try all 2^n truth assignments.
- Q. Can we do anything substantially more clever? Conjecture. No poly-time algorithm for SAT.

"intractable"



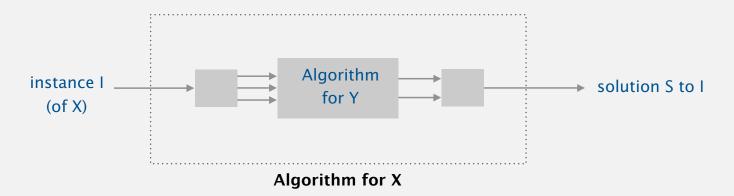
Classifying problems

- Q. Which search problems are in P?
- A. No easy answers (we don't even know whether P = NP).



Problem *X* poly-time reduces to problem *Y* if *X* can be solved with:

- Polynomial number of standard computational steps.
- Polynomial number of calls to Y.



Consequence. If SAT poly-time reduces to *Y*, then we conclude that *Y* is (probably) intractable.

SAT poly-time reduces to ILP

SAT. Given a system of boolean equations, find a solution.

$$x'_1 ext{ or } x_2 ext{ or } x_3 = true$$
 $x_1 ext{ or } x'_2 ext{ or } x_3 = true$
 $x'_1 ext{ or } x'_2 ext{ or } x'_3 = true$
 $x'_1 ext{ or } x'_2 ext{ or } x_4 = true$

can to reduce any SAT problem to this form

ILP. Given a system of linear inequalities, find a 0-1 solution.

$$1 \le (1 - x_1) + x_2 + x_3$$

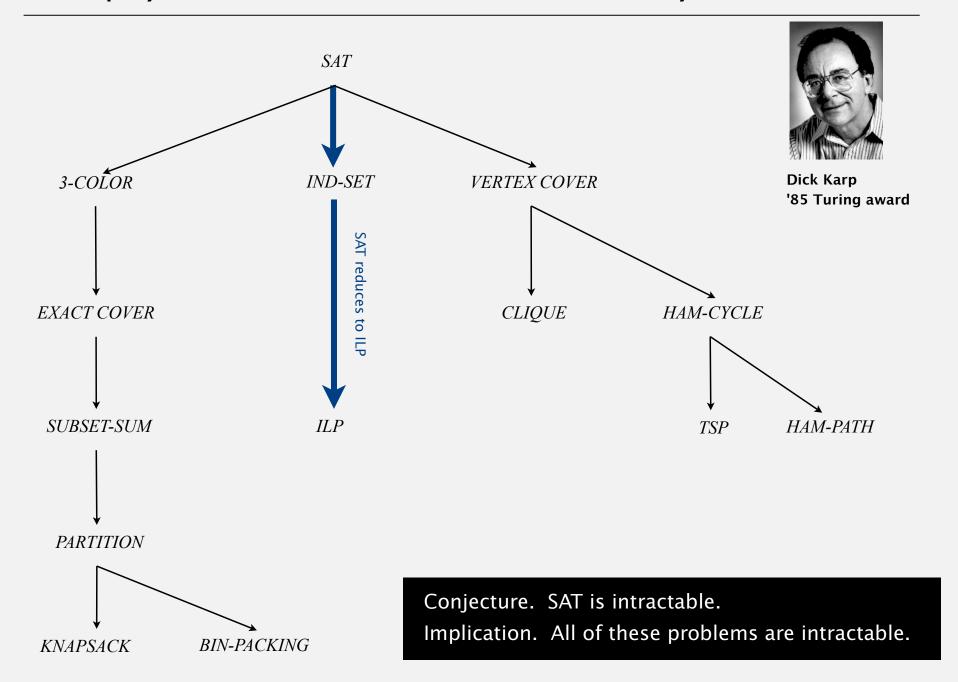
$$1 \le x_1 + (1 - x_2) + x_3$$

$$1 \le (1 - x_1) + (1 - x_2) + (1 - x_3)$$

$$1 \le (1 - x_1) + (1 - x_2) + x_4$$

solution to this ILP instance gives solution to original SAT instance

More poly-time reductions from boolean satisfiability



Still more reductions from SAT

Aerospace engineering. Optimal mesh partitioning for finite elements.

Biology. Phylogeny reconstruction.

Chemical engineering. Heat exchanger network synthesis.

Chemistry. Protein folding.

Civil engineering. Equilibrium of urban traffic flow.

Economics. Computation of arbitrage in financial markets with friction.

Electrical engineering. VLSI layout.

Environmental engineering. Optimal placement of contaminant sensors.

Financial engineering. Minimum risk portfolio of given return.

Game theory. Nash equilibrium that maximizes social welfare.

Mathematics. Given integer a_1 , ..., a_n , compute $\int_0^{2\pi} \cos(a_1\theta) \times \cos(a_2\theta) \times \cdots \times \cos(a_n\theta) d\theta$

Mechanical engineering. Structure of turbulence in sheared flows.

Medicine. Reconstructing 3d shape from biplane angiocardiogram.

Operations research. Traveling salesperson problem.

Physics. Partition function of 3d Ising model.

Politics. Shapley-Shubik voting power.

Recreation. Versions of Sudoko, Checkers, Minesweeper, Tetris.

Statistics. Optimal experimental design.



- introduction
- search problems
- Pvs. NP
- classifying problems
- NP-completeness
- coping with intractability

Algorithms

ROBERT SEDGEWICK | KEVIN WAYNE



introduction

search problems

P vs. NP

classifying problems

NP-completeness

coping with intractability

Algorithms

ROBERT SEDGEWICK | KEVIN WAYNE

NP-completeness

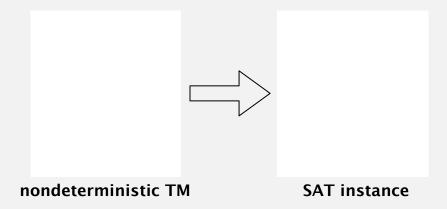
Def. An NP problem is NP-complete if every problem in NP poly-time reduce to it.

Proposition. [Cook 1971, Levin 1973] SAT is NP-complete.

every NP problem is a SAT problem in disguise

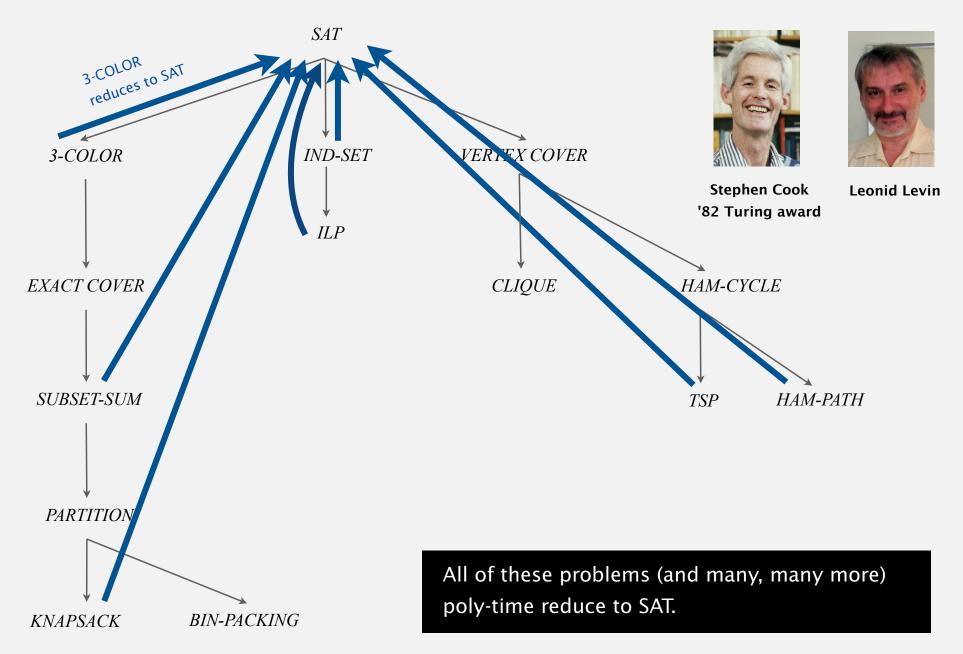
Extremely brief proof sketch:

- Convert non-deterministic TM notation to SAT notation.
- If you can solve SAT, you can solve any problem in NP.

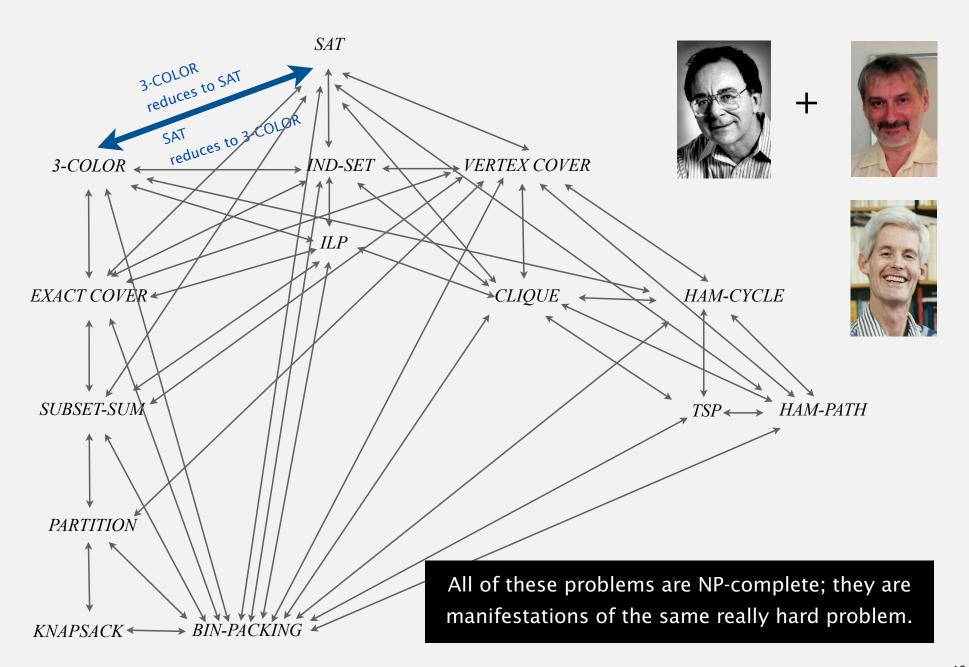


Corollary. Poly-time algorithm for SAT iff P = NP.

Implications of Cook-Levin theorem



Implications of Karp + Cook-Levin



Implications of NP-Completeness

Implication. [SAT captures difficulty of whole class NP]

- Poly-time algorithm for SAT iff P = NP.
- No poly-time algorithm for some NP problem ⇒ none for SAT.

Remark. Can replace SAT with any of Karp's problems.

Proving a problem NP-complete guides scientific inquiry.

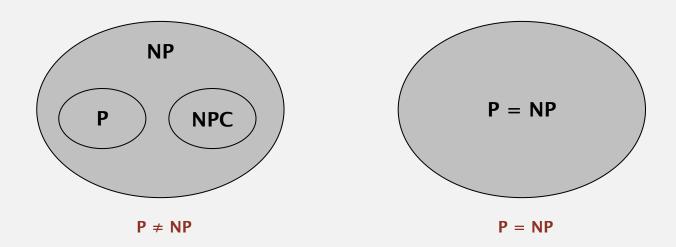
- 1926: Ising introduces simple model for phase transitions.
- 1944: Onsager finds closed form solution to 2D version in tour de force.
- 19xx: Feynman and other top minds seek 3D solution.
- 2000: 3D-ISING proved NP-complete.

a holy grail of statistical mechanics

search for closed formula appears doomed

Two worlds (more detail)

Overwhelming consensus (still). $P \neq NP$.



Why we believe $P \neq NP$.

"We admire Wiles' proof of Fermat's last theorem, the scientific theories of Newton, Einstein, Darwin, Watson and Crick, the design of the Golden Gate bridge and the Pyramids, precisely because they seem to require a leap which cannot be made by everyone, let alone a by simple mechanical device." — Avi Wigderson

Summary

P. Class of search problems solvable in poly-time.

NP. Class of all search problems, some of which seem wickedly hard.

NP-complete. Hardest problems in NP.

Intractable. Problem with no poly-time algorithm.

Many fundamental problems are NP-complete.

- SAT, ILP, HAMILTON-PATH, ...
- 3D-ISING, ...

Use theory a guide:

- A poly-time algorithm for an NP-complete problem would be a stunning breakthrough (a proof that P = NP).
- You will confront NP-complete problems in your career.
- Safe to assume that $P \neq NP$ and that such problems are intractable.
- Identify these situations and proceed accordingly.



introduction

search problems

P vs. NP

classifying problems

NP-completeness

coping with intractability

Algorithms

ROBERT SEDGEWICK | KEVIN WAYNE



- introduction
- search problems
- PVS. NP
- classifying problems
- NP-completeness
- coping with intractability

Algorithms

ROBERT SEDGEWICK | KEVIN WAYNE

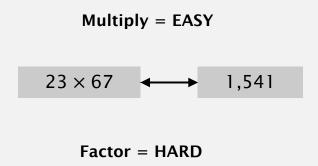
Exploiting intractability

Modern cryptography.

- Ex. Send your credit card to Amazon.
- · Ex. Digitally sign an e-document.
- Enables freedom of privacy, speech, press, political association.

RSA cryptosystem.

- To use: multiply two *n*-bit integers. [poly-time]
- To break: factor a 2 *n*-bit integer. [unlikely poly-time]



Exploiting intractability

Challenge. Factor this number.

740375634795617128280467960974295731425931888892312890849362 326389727650340282662768919964196251178439958943305021275853 701189680982867331732731089309005525051168770632990723963807 86710086096962537934650563796359

RSA-704 (\$30,000 prize if you can factor)

Can't do it? Create a company based on the difficulty of factoring.

P & Q PRIME N = PQED = 1 MOD (P-1)(Q-1) $C = M^c$ ANOD N $M = C^b$ MOD NThe RSA algorithm is the

most widely used method of implementing public key cryptography and has been deployed in more than one billion applications worldwide.

RSA algorithm



RSA sold for \$2.1 billion



or design a t-shirt

Exploiting intractability

FACTOR. Given an *n*-bit integer *x*, find a nontrivial factor.

- Q. What is complexity of FACTOR?
- A. In NP, but not known (or believed) to be in P or NP-complete.
- O. What if P = NP?
- A. Poly-time algorithm for factoring; modern e-conomy collapses.

Proposition. [Shor 1994] Can factor an n-bit integer in n^3 steps on a "quantum computer."

Q. Do we still believe the extended Church-Turing thesis???



Coping with intractability

Relax one of desired features.

- Solve arbitrary instances of the problem.
- Solve the problem to optimality.
- Solve the problem in poly-time.

Special cases may be tractable.

- Ex: Linear time algorithm for 2-SAT. ← at most two variables per equation
- Ex: Linear time algorithm for Horn-SAT. ← at most one un-negated variable per equation

Coping with intractability

Relax one of desired features.

- Solve arbitrary instances of the problem.
- Solve the problem to optimality.
- Solve the problem in poly-time.

Develop a heuristic, and hope it produces a good solution.

- No guarantees on quality of solution.
- Ex. TSP assignment heuristics.
- Ex. Metropolis algorithm, simulating annealing, genetic algorithms.

Approximation algorithm. Find solution of provably good quality.

• Ex. MAX-3SAT: provably satisfy 87.5% as many clauses as possible.



but if you can guarantee to satisfy 87.51% as many clauses as possible in poly-time, then P = NP!

Coping with intractability

Relax one of desired features.

- Solve arbitrary instances of the problem.
- Solve the problem to optimality.
- Solve the problem in poly-time.

Complexity theory deals with worst case behavior.

- Instance(s) you want to solve may be "easy."
- Chaff solves real-world SAT instances with ~ 10K variable.

Chaff: Engineering an Efficient SAT Solver

Matthew W. Moskewicz Department of EECS UC Berkeley Conor F. Madigan Department of EECS MIT Ying Zhao, Lintao Zhang, Sharad Malik Department of Electrical Engineering Princeton University

moskewcz@alumni.princeton.edu

cmadigan@mit.edu

{yingzhao, lintaoz, sharad}@ee.princeton.edu

ABSTRACT

Boolean Satisfiability is probably the most studied of combinatorial optimization/search problems. Significant effort has been devoted to trying to provide practical solutions to this problem for problem instances encountered in a range of applications in Electronic Design Automation (EDA), as well as in Artificial Intelligence (AI). This study has culminated in the

Many publicly available SAT solvers (e.g. GRASP [8], POSIT [5], SATO [13], rel_sat [2], WalkSAT [9]) have been developed, most employing some combination of two main strategies: the Davis-Putnam (DP) backtrack search and heuristic local search. Heuristic local search techniques are not guaranteed to be complete (i.e. they are not guaranteed to find a satisfying assignment if one exists or prove unsatisfiability); as a

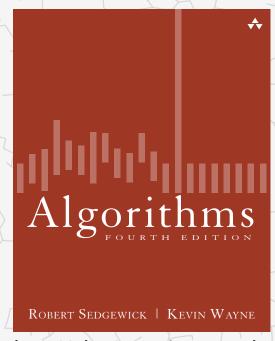


- introduction
- search problems
- PVS. NP
- classifying problems
- NP-completeness
- coping with intractability

Algorithms

ROBERT SEDGEWICK | KEVIN WAYNE

Algorithms



http://algs4.cs.princeton.edu

6.6 INTRACTABILITY

- introduction
- search problems
- Pvs. NP
- classifying problems
- NP-completeness
- coping with intractability